Strength Design

• TMS Chap 9

Frank Lloyd Wright's iconic Ennis House sells for a record-setting \$18 million





Photo: Mary E. Nichols, via Realtor.com

Slide 1 of 35

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Ennis House - Frank Loyd Wright



Masonry

After an incredible publicity blitz and well over a year on the market, Frank Lloyd Wright's world-renowned Ennis House tucked into the foothills of Los Feliz [...] — has sold for \$18 million to an as-yet-unidentified buyer. That number, while significantly below the \$23 million ask, ranks it as the priciest Wrightdesigned home ever sold, easily eclipsing the previous high-water mark set by the Storer House in nearby Hollywood Hills, which was purchased in 2013 for \$6.8 million [...] — Variety



Ennis House – Frank Loyd Wright





University of Michigan, TCAUP

Ennis House - Frank Loyd Wright



Design Options

Empirical

• TMS 402 Appendix A

Allowable Stress Design (ASD)

• TMS 402 Chap. 8

Strength Design

• TMS 402 Chap. 9



Design Options

Empirical

TMS 402 Appendix A

Allowable Stress Design (ASD)

• TMS 402 Chap. 8

Strength Design

- TMS 402 Chap. 9
- IBC Section 2108
 - mostly references TMS 402
 - steel development length capped at 72 d_b
 - Mechanical and welded splices





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Slide 7 of 35

TMS 402

Development



- 9.1 General
- 9.1.1 Scope
- 9.1.2 Required strength
- 9.1.3 Design strength
- 9.1.4 Strength-reduction factors
- 9.1.5 Deformation requirements
- 9.1.6 Anchor bolts embedded in grout
- 9.1.7 Shear strength in Multiwythe elements
- 9.1.8 Nominal bearing strength
- 9.1.9 Material properties



TMS 402 Chapter 9

Strength Design Method

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Strength Required by Loads < Strength of Masonry

Masonry

γPu > øPn

- 1.2 D + 1.6 Lr + 0.5(Lr or S)
- 1.2 D + 1.6(Lr or S) + (L or 0.5W)
- 1.2 D + 1.0W + L + 0.5(Lr or S)
- 0.9D + 1.0W
- 1.2D + Ev + Eh + L + 0.2S
- 0.9D Ev + Eh

(Equation 9-11) for h/r < 99

$$P_n = 0.80 \left\{ 0.80 A_n f'_m \left[1 - \left(\frac{h}{140r}\right)^2 \right] \right\}$$

$$P_n = 0.80 \left[0.80 A_n f'_m \left(\frac{70 r}{h} \right)^2 \right]$$

9.1.4 Strength-reduction factors, ø

| Action | Reinforced Masonry | Unreinforced Masonry |
|--|-----------------------|-------------------------|
| combinations of flexure and axial load | 0.90 | 0.60 |
| shear | 0.8 | 30 |
| bearing | 0.0 | 50 |
| anchor bolts: pryout | 0.! | 50 |
| anchor bolts: controlled by anchor bolt steel | 0.9 | 90 |
| anchor bolts: pullout | 0.6 | 65 |
| | | |

Masonry

Slide 11 of 35

TMS 402 Chapter 9 Strength Design $Pu \le Pn$

Section 9.2 Unreinforced (plain) masonry

9.2.1 Scope

- 9.2.2 Design criteria (uncracked)
- 9.2.3 Design assumptions
- strain proportional to distance from N.A.
- flexural tension proportional to strain
- flexural comp. + axial comp. proportional to strain
- stresses in reinforcement are not accounted for

9.2.4 Nominal flexural and axial strength

- compressive stress ≤ 0.80 f'm
- tensile stress \leq fr
- 9.2.5 Axial tension
- tension resistance shall be neglected
- 9.2.6 Nominal shear strength (3.8 Anv √f'm or 300 Anv)

$$f_t = \frac{Mc}{I} - \frac{P}{A}$$

(Equation 9-11) for h/r < 99
$$P_n = 0.80 \left\{ 0.80 A_n f'_m \left[1 - \left(\frac{h}{140r}\right)^2 \right] \right\}$$

(Equation 9-12) for h/r > 99

$$P_n = 0.80 \left[0.80 A_n f'_m \left(\frac{70 r}{h} \right)^2 \right]$$

Table 9.1.9.2 Modulus of Rupture

| Masonry Type | Mortar Type | | | | | |
|---|------------------------|------------------------------|------------|---------------|--|--|
| | Por cemen mortar | tland t/lime or cement | Masonry | Cement | | |
| | M or S | Ν | M or S | Ν | | |
| Normal to Bed Joints Solid Units | 133 | 100 | 80 | 51 | | |
| Hollow Units ¹ Ungrouted Fully Grouted | 84 163 | 64 158 | 51 153 | 31 145 | | |
| Parallel to bed joints in running bond Solid Units Hollow Units | 267 | 200 | 160 | 100 | | |
| Ungrouted and partially grouted Fully grouted | 167 267 | 127 200 | 100 160 | 64 100 | | |
| Parallel to bed joints not laid in running bond Continuous grout section parallel to bed joints | 335 | 335 | 335 | 335 | | |
| Other | 0 | 0 | 0 | 0 | | |
| University of Michigan, TCAUP Masonr | / | | s | lide 13 of 35 | | |

Reinforced Masonry Analysis - procedure

for axial compression using TMS 402 (2016) Strength Design (LRFD) – **non-reinforced**

Given: applied load, geometry, material Find: axial compressive load capacity, Pn

- 1. Determine the masonry strength, f'm, based on unit strength, fu, and mortar type
- 2. Find the net area, A_n , and r (see TEK 14-1B)
- 3. Calculate h/r
- 4. Choose the axial strength equation, Pn: If $h/_r < 99$ use TMS 402 eq.9-11 If $h/_r > 99$ use TMS 402 eq.9-12
- 6. Check that øPn is greater than Pu.

(Equation 9-11) for h/r < 99

$$P_n = 0.80 \left\{ 0.80 A_n f'_m \left[1 - \left(\frac{h}{140r}\right)^2 \right] \right\}$$

(Equation 9-12) for h/r > 99

$$P_n = 0.80 \left[0.80 A_n f'_m \left(\frac{70 r}{h} \right)^2 \right]$$

Masonry Strength

TMS 602 – Table 2 – s18

Masonry strength, f'm, based on unit strength,

fu, and mortar type M, S or N



Concrete Masonry

| Table 2 — C | ompress | sive | strengtl | n of | mas | sonry | base | d on | tł | ne com | pressi | ive |
|-------------|---------------------|------|----------|------|------|-------|------|------|----|--------|--------|-----|
| st | trength onstruct | of o | concrete | maso | onry | units | and | type | of | mortar | used | in |

| Net area compressive strength of | Net area compressive strength of ASTM C90 concrete masonry <u>units</u> , psi (MPa) | | | | |
|---|--|---------------|--|--|--|
| concrete masonry, psi $(MPa)^1 \qquad f'm$ | Type M or S mortar | Type N mortar | | | |
| 1.750 (12.07) | | 2,000 (13.79) | | | |
| 2,000 (13,79) | 2,000 (13.79) | 2,650 (18.27) | | | |
| 2.250 (15.51) | 2,600 (17.93) | 3,400 (23.44) | | | |
| 2,200 (17,24) | 3,250 (22.41) | 4,350 (28.96) | | | |
| 2,750 (18.96) | 3,900 (26.89) | | | | |
| 3,000 (20.69) | 4,500 (31.03) | | | | |

¹ For units of less than 4 in. (102 mm) nominal height, use 85 percent of the values listed.

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Structures II

Slide 15 of 35

Reinforced Masonry Analysis

for axial compression using TMS 402 (2016) Strength Design – **non-reinforced**

Section Properties of Concrete Masonry Walls TEK 14 - 1B



Reinforced Masonry Analysis

for axial compression using TMS 402 (2016) Strength Design – **non-reinforced**

Section Properties of Concrete Masonry Walls TEK 14 - 1B

| | Grout | Mortar | Net cros | s-sectional p | propertiesA | |
|--------------------|--------------------|------------|------------------------------|------------------------------|------------------------------|---|
| Unit | spacing (in.) | bedding | A_n (in. ² /ft) | I_n (in. ⁴ /ft) | S_n (in. ³ /ft) | |
| A Hollow | No grout | Face shell | 30.0 | 308.7 | 81.0 | Ī |
| B Hollow | No grout | Full | 41.5 | 334.0 | 87.6 | |
|)/E 00% sol | id/solidly grouted | Full | 91.5 | 443.3 | 116.3 | |
| C Hollow | 16 | Face shell | 62.0 | 378.6 | 99.3 | |
| Hollow | 24 | Face shell | 51.3 | 355.3 | 93.2 | |
| Hollow | 32 | Face shell | 46.0 | 343.7 | 90.1 | |
| Hollow | 40 | Face shell | 42.8 | 336.7 | 88.3 | |
| Hollow | 48 | Face shell | 40.7 | 332.0 | 87.1 | |
| Hollow | 72 | Face shell | 37.1 | 324.3 | 85.0 | |
| Hollow | 96 | Face shell | 35.3 | 320.4 | 84.0 | |
| Hollow | 120 | Face shell | 34.3 | 318.0 | 83.4 | |

Table 3—8-inch (203-mm) Single Wythe Walls, 1¹/₄ in. (32 mm) Face Shells (standard)

Reinforced Masonry Analysis

for axial compression using TMS 402 (2016) Strength Design – **non-reinforced**



Reinforced Masonry Analysis

for axial compression using TMS 402 (2016) Strength Design – **non-reinforced**

2. Find the net area, A_n , and radius of gyration, r_{avg} (see TEK 14-1B)

| | | Grout | Mortar | Net cros | ss-sectional p | propertiesA | Avera | ige cross-sec | tional proper | ties ^B |
|---------------|-------------|--------------------|--------------|------------------------------|--------------------------------|------------------------------|----------------------------------|----------------|----------------------------------|-------------------|
| | Unit | spacing (in.) | bedding | A_n (in. ² /ft) | I_{n} (in. ⁴ /ft) | S_n (in. ³ /ft) | A_{avg} (in. ² /ft) | Iavg (in.4/ft) | S_{avg} (in. ³ /ft) | r_{ang} (in.) |
| | Hollow | No grout | Face shell | 30.0 | 308.7 | 81.0 | 41.5 | 334.0 | 87.6 | 2.84 |
| | Hollow | No grout | Full | 41.5 | 334.0 | 87.6 | 41.5 | 334.0 | 87.6 | 2.84 |
| | 100% sol | id/solidly grouted | Full | 91.5 | 443.3 | 116.3 | 91.5 | 443.3 | 116.3 | 2.20 |
| | Hollow | 16 | Face shell | 62.0 | 378.6 | 99.3 | 65.8 | 387.1 | 101.5 | 2.43 |
| | Hollow | 24 | Face shell | (51.3) | 355.3 | 93.2 | 57.7 | 369.4 | 96.9 | 2.53 |
| | Hollow | 32 | Face shell | 46.0 | 343.7 | 90.1 | 53.7 | 360.5 | 94.6 | 2.59 |
| | Hollow | 40 | Face shell | 42.8 | 336.7 | 88.3 | 51.2 | 355.2 | 93.2 | 2.63 |
| | Hollow | 48 | Face shell | 40.7 | 332.0 | 87.1 | 49.6 | 351.7 | 92.2 | 2.66 |
| | Hollow | 72 | Face shell | 37.1 | 324.3 | 85.0 | 46.9 | 345.8 | 90.7 | 2.71 |
| | Hollow | 96 | Face shell | 35.3 | 320.4 | 84.0 | 45.6 | 342.8 | 89.9 | 2.74 |
| | Hollow | 120 | Face shell | 34.3 | 318.0 | 83.4 | 44.8 | 341.0 | 89.5 | 2.76 |
| | | | 3b: Vertical | Section Pr | operties (M | asonry Spar | nning Horiz | ontally) | | |
| | Hollow | No grout | Face shell | 30.0 | 308.7 | 81.0 | 40.5 | 330.1 | 86.6 | 2.86 |
| | Hollow | No grout | Full | 30.0 | 308.7 | 81.0 | 41.5 | 334.0 | 87.6 | 2.84 |
| | 100% sol | id/solidly grouted | Full | 91.5 | 443.3 | 116.3 | 91.5 | 443.3 | 116.3 | 2.20 |
| | Hollow | 16 | Face shell | 60.8 | 376.0 | 98.6 | 71.2 | 397.4 | 104.2 | 2.36 |
| | Hollow | 24 | Face shell | 50.5 | 353.6 | 92.7 | 61.0 | 374.9 | 98.3 | 2.48 |
| | Hollow | 32 | Face shell | 45.4 | 342.4 | 89.8 | 55.8 | 363.7 | 95.4 | 2.55 |
| | Hollow | 40 | Face shell | 42.3 | 335.6 | 88.0 | 52.8 | 357.0 | 93.6 | 2.60 |
| | Hollow | 48 | Face shell | 40.3 | 331.1 | 86.9 | 50.7 | 352.5 | 92.5 | 2.64 |
| | Hollow | 96 | Face shell | 35.1 | 319.9 | 83.9 | 45.6 | 341.3 | 89.5 | 2.74 |
| | Hollow | 120 | Face shell | 34.1 | 317.7 | 83.3 | 44.6 | 339.0 | 88.9 | 2.76 |
| | Ō | Table 3—8- | inch (20 | 3-mm) Si | ngle WytH (standa | ne Walls, ard) | 1% in. | (32 mm) | Face Shel | ls |
| versity of Mi | chigan, TCA | NUP | | | Structure | es II | | | | Slide 19 of 3 |

Reinforced Masonry Analysis

for axial compression using TMS 402 (2016) Strength Design – **non-reinforced**

3. Calculate h/r3. Calculate h/rA_n = 51.3 in² $F_{ovg} = 2.53$ in $h/r = \frac{12}{2.53}$ i



Interaction Diagram



Moment Magnification

Design for magnified moment: $M_u = \psi M_{u,0}$



- Can take $\psi = 1$ if $h/r \le 45$
- Can take $\psi = 1$ if $45 < h/r \le 60$ and nominal strength reduced by 10%



Masonry

Slide 23 of 35

Unreinforced Masonry Wall example

Given: h = 12 ft t = 8 in hollow CMU, fu = 2000 psi type S mortar, face shell bedding, no grout

Loading: D = 1 k/ft + selfweight of 30 psf Lr = 0.5 k/ft (w/ e=3 in.)W = 24 psf (+ or -)

 $\frac{\text{Load Combinations}}{1.4\text{D}}$ $1.2\text{D} + 1.6\text{L}_{r}$ $1.2\text{D} + 1.0\text{W} + 0.5\text{L}_{r}$ $0.9\text{D} + 1.0\text{W} \quad \text{sc}$





Unreinforced Masonry Wall

example

Section Properties of Concrete Masonry Walls TEK 14 - 1B





Unreinforced Masonry Wall example

| | Grout | Mortar | Net cros | s-sectional p | propertiesA | Avera | ge cross-sec | tional proper | ties ^B |
|---------|---------------------|-------------|------------------------------|---------------|------------------------------|----------------------------------|----------------|----------------------------------|-------------------|
| Unit | spacing (in.) | bedding | A_n (in. ² /ft) | I. (in.4/ft) | S_n (in. ³ /ft) | A_{avg} (in. ² /ft) | Iavg (in.4/ft) | S_{avg} (in. ³ /ft) | rave (in. |
| Hollow | No grout | Face shell | 30.0 | 308.7 | 81.0 | 41.5 | 334.0 | 87.6 | 2.84 |
| Hollow | No grout | Full | 41.5 | 334.0 | 87.6 | 41.5 | 334.0 | 87.6 | 2.84 |
| 100% so | lid/solidly grouted | Full | 91.5 | 443.3 | 116.3 | 91.5 | 443.3 | 116.3 | 2.20 |
| Hollow | 16 | Face shell | 62.0 | 378.6 | 99.3 | 65.8 | 387.1 | 101.5 | 2.43 |
| Hollow | 24 | Face shell | 51.3 | 355.3 | 93.2 | 57.7 | 369.4 | 96.9 | 2.53 |
| Hollow | 32 | Face shell | 46.0 | 343.7 | 90.1 | 53.7 | 360.5 | 94.6 | 2.59 |
| Hollow | 40 | Face shell | 42.8 | 336.7 | 88.3 | 51.2 | 355.2 | 93.2 | 2.63 |
| Hollow | 48 | Face shell | 40.7 | 332.0 | 87.1 | 49.6 | 351.7 | 92.2 | 2.66 |
| Hollow | 72 | Face shell | 37.1 | 324.3 | 85.0 | 46.9 | 345.8 | 90.7 | 2.71 |
| Hollow | 96 | Face shell | 35.3 | 320.4 | 84.0 | 45.6 | 342.8 | 89.9 | 2.74 |
| Hollow | 120 | Face shell | 34.3 | 318.0 | 83.4 | 44.8 | 341.0 | 89.5 | 2.76 |
| | | 3b: Vertica | Section Pro | operties (Ma | asonry Spar | ning Horizo | ontally) | | |
| Hollow | No grout | Face shell | 30.0 | 308.7 | 81.0 | 40.5 | 330.1 | 86.6 | 2.86 |
| Hollow | No grout | Full | 30.0 | 308.7 | 81.0 | 41.5 | 334.0 | 87.6 | 2.84 |
| 100% so | lid/solidly grouted | Full | 91.5 | 443.3 | 116.3 | 91.5 | 443.3 | 116.3 | 2.20 |
| Hollow | 16 | Face shell | 60.8 | 376.0 | 98.6 | 71.2 | 397.4 | 104.2 | 2.36 |
| Hollow | 24 | Face shell | 50.5 | 353.6 | 92.7 | 61.0 | 374.9 | 98.3 | 2.48 |
| Hollow | 32 | Face shell | 45.4 | 342.4 | 89.8 | 55.8 | 363.7 | 95.4 | 2.55 |
| Hollow | 40 | Face shell | 42.3 | 335.6 | 88.0 | 52.8 | 357.0 | 93.6 | 2.60 |
| Hollow | 48 | Face shell | 40.3 | 331.1 | 86.9 | 50.7 | 352.5 | 92.5 | 2.64 |
| Hollow | 96 | Face shell | 35.1 | 319.9 | 83.9 | 45.6 | 341.3 | 89.5 | 2.74 |
| Hollow | 120 | Face shell | 34.1 | 317.7 | 83.3 | 44.6 | 339.0 | 88.9 | 2.76 |



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Masonry

Slide 27 of 35

Unreinforced Masonry Wall example

Load Combinations

 $\begin{array}{l} 1.4D \\ 1.2D + 1.6L_r \\ 1.2D + 1.0W + 0.5L_r \\ 0.9D + 1.0W \end{array}$

Determine the controlling load combination

- B. $1.2D + 1.0W + 0.5L_r$ Wind suction (compression on inside)
- C. 0.9D + 1.0W Wind pressure (compression on outside)
- D. 0.9D + 1.0W

Wind suction (compression on inside)

| Load Combination | Tensile Stress (psi) |
|---|----------------------|
| 1.2D + 1.0W + 0.5L _r wind pressure | ? |
| 1.2D + 1.0W + $0.5L_r$ wind suction | ? |
| 0.9D + 1.0W wind pressure | ? |
| 0.9D + 1.0W wind suction | ? |

Unreinforced Masonry Wall example

Load Combinations

 $\begin{array}{l} 1.4D \\ 1.2D + 1.6L_r \\ 1.2D + 1.0W + 0.5L_r \\ 0.9D + 1.0W \end{array}$

Determine the controlling load combination

| A. $1.2D + 1.0W + 0.5L_r$ V | Wind pressure (| (compression on | outside) |
|-----------------------------|-----------------|-----------------|----------|
|-----------------------------|-----------------|-----------------|----------|

- B. $1.2D + 1.0W + 0.5L_r$ Wind suction (compression on inside)
- C. 0.9D + 1.0W Wind pressure (compression on outside)
- D. 0.9D + 1.0W Wind suction (compression on inside)

| | Load Combination | Tensile Stress (psi) |
|----------|---|----------------------|
| | 1.2D + 1.0W + 0.5L _r wind pressure | 5.9 psi |
| | 1.2D + 1.0W + 0.5L _r wind suction | 40.4 psi |
| | 0.9D + 1.0W wind pressure | 12.4 psi |
| X | 0.9D + 1.0W wind suction | 47.6 psi |
| | | |
| Universi | ity of Michigan, TCAUP Masonry | Slide 29 |

Unreinforced Masonry Wall example

Given: h = 12 ft t = 8 in hollow CMU, fu = 2000 psi

type S mortar, face shell bedding, no grout

Loading:

D = 1 k/ft + selfweight of 30 psfLr = 0.5 k/ft (w/ e=3 in.) W = 24 psf (+ or -)



Unreinforced Masonry Wall example



Unreinforced Masonry Wall example

0.9D + 1.0W - Wind suction (compression on inside face of wall)

Location of max
moment, x
$$x = \frac{h}{2} - \frac{M_{uf}}{w_u h} = \frac{144in}{2} - \frac{2700 \frac{lb \cdot in}{ft}}{24 \frac{lb}{ft^2} (12ft)} = 62.6in.$$
Factored axial
load, P_u

$$P_u = 0.9 \left(\underbrace{1000 \frac{lb}{ft} + 30 \frac{lb}{ft^2} \left(\frac{62.6in}{12in./ft} \right)}_{W_u f} \right) = \underbrace{1041 \frac{lb}{ft}}_{ft}$$

$$\underbrace{E_{CCLJTRAC}}_{Muf}$$
Muf = $P_{uf}e = 0.9 \left(\underbrace{1000 \frac{lb}{ft}}_{ft} \right) (3.0in.) = \underbrace{2700 \frac{lb \cdot in}{ft}}_{ft}$
Maximum combined
moment, $M_{u,0}$

$$M_{u,0} = \frac{M_{uf}}{2} + \frac{W_u h^2}{8} + \frac{M_{uf}^2}{2W_u h^2}$$

$$= \frac{2700\frac{lb \cdot in.}{ft}}{2} + \frac{24\frac{lb}{ft^2}(12ft)^2 \left(12\frac{in.}{ft}\right)}{8} + \frac{\left(2700\frac{lb \cdot in.}{ft}\right)^2}{2\left(24\frac{lb}{ft^2}\right)(12ft)^2 \left(12\frac{in.}{ft}\right)}$$

= 1350 + 5184 + 88 = $\underbrace{6622}_{ft} \underbrace{lb \cdot in.}_{ft}$
Masonry Slide 32 of 35

.



| Unrei 0.9D | nforced Masonry Wall example + 1.0W - Wind suction (compression on inside face of wall) | |
|---------------|---|----------------|
| Wł | nat to do to make wall work? (short of reinforcing wall) | |
| 1. | Increase wall size, say to 12 in. (Sn = 139.6 in³/ft). Maximu tensile stress is 12.7 psi. | m |
| 2. | Grout wall. (w-wall = 75 psf; An = 91.5 in ² /ft; Sn = 116.3 in ³ / f_r = 163 psi) Maximum tensile stress of 45.3 psi is less than design stress of 0.6(163) = 97.8 psi | ft; |
| 3. | Use Portland cement/lime or mortar cement (modulus of rup is 84 psi). Maximum tensile stress of 47.2 psi is less than de stress of 0.6(94)=50.4 psi | oture esign |
| 4. | Use pilasters | |
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